



Energy-Efficient Reversible Full Adder and Ripple Carry Adder Architecture for Modern Digital Systems

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Abstract:

Arithmetic primitives play a critical role in performing computations on large numbers, particularly in arithmetic circuit implementations that involve operations like multiplication, addition, subtraction, and division. Given the significance of computations in central processing units (CPUs), optimizing the design of arithmetic circuits has been a key area of research for engineers. In the pursuit of developing energy-efficient, low-power portable processors for applications such as image processing, digital signal processing, and cryptography, it's essential to minimize factors like switching activity and cell count. This research focuses on the design of a reversible binary full adder circuit, a crucial component in evaluating the Energy Delay Product (EDP) for a variety of computing applications. The study introduces a novel reversible binary full adder based on the concepts of switching activity and logic decomposition. The fundamental building blocks for reversible full adders—such as Feynman Gates, Toffoli Gates and New Gates—are designed first. Then, leveraging these components, a new reversible binary full adder is developed using the proposed method. The results show that the proposed reversible full adder outperforms existing designs in terms of dynamic power dissipation. Additionally, a formula-based evaluation is conducted on the implementation results to estimate the EDP, which reveals a 32.3% improvement in EDP compared to the previously proposed full adder design.

Keywords: — Arithmetic Primitives, Reversible Digital Full Adder, Energy Delay Product (EDP), Low-Power Circuit Design, Switching Activity Factor, Reversible Logic Gates

I. INTRODUCTION:

Reducing dynamic power consumption is a fundamental goal in modern digital logic design. This paper presents a new approach to creating a low-power full adder circuit, leveraging the benefits of reversible logic for energy efficiency. Reversible logic has gained attention as a promising solution for designing digital systems that consume less power. The proposed architecture incorporates optimized reversible gates to reduce power dissipation in the full adder circuit. A key component of this design is the innovative 4×4 reversible gate, named FADE, which plays a pivotal role in reducing energy usage. The use of reversible logic in this context has significant implications for quantum computing, where traditional logic is limited by constraints such as the lack of feedback and the need for reversibility.

The report also delves into the implementation of fundamental arithmetic circuits such as adders, subtractors and multipliers. Notable advancements in this field involve the use of 3×3 reversible gates integrated with quantum-dot cellular automata (QCA). These developments offer a path to building more efficient and scalable digital systems. However, when designing high-performance processors, heat dissipation becomes a critical issue, limiting the potential for increasing computational accuracy without causing thermal instability. Cryptographic algorithms, often evaluated based on hardware efficiency metrics like gate count, benefit significantly from the energy-saving properties of reversible logic. Despite its advantages, designing reversible combinational circuits is more complex than traditional methods due to the limitations imposed by reversibility, such as the prohibition of fan-out and feedback.

One of the recent innovations in the field is the integration of 3×3 reversible gates with quantum-dot cellular automata (QCA), which can lead to more efficient and compact designs. These advancements are particularly important in addressing the challenges of thermal management in high-performance processors. While the cost of manufacturing embedded systems may rise over time, managing dynamic power consumption remains a priority in today's digital landscape. This makes the need for reversible logic increasingly critical, as it offers significant power savings, especially in applications such as low-power circuit design. A new approach for optimizing the performance of reversible full adder and subtractor circuits is also presented, focusing on minimizing the number of logic cells required.

Incorporating reversible logic allows for the reduction of circuit component sizes to the microscopic scale, which is essential for modern device accessibility. A notable example is the Quantum-Dot Cellular Automata (QCA) design, which provides ultra-efficient full adders through the interaction of cells. This method demonstrates substantial improvements over conventional digital circuits using reversible logic. While the upfront costs of embedded systems may rise, the focus today is on reducing dynamic power consumption and optimizing trade-offs. This paper also highlights the design of a fault-tolerant full adder based on parity-preserving logic, which has become crucial for minimizing power loss in VLSI circuits. Overall, the development of reversible logic circuits offers significant potential for future advancements in low-power, high-efficiency digital design.

II. EXISTING METHOD:

A full adder circuit is designed using Verilog HDL, leveraging fundamental logic components like AND and OR gates. The circuit simulation and implementation are conducted on the Xilinx development platform. Traditional digital circuit design relies on irreversible logic gates, such as AND, OR, and XOR gates, which often result in power dissipation and increased propagation delays. These limitations affect both speed and energy efficiency of the circuits. As a result, more optimized techniques are being sought to reduce energy loss and improve performance.

The basic logic gates employed in this design include the AND gate and OR gate, both essential for performing binary operations in digital circuits. The AND gate outputs a high signal only when all its inputs are high, whereas the OR gate produces a high output if any input is high. These gates form the fundamental building blocks for the more complex operations carried out by the full adder. However, the use of these conventional gates has inherent energy inefficiencies, primarily due to the irreversible nature of the logic, which contributes to unnecessary energy dissipation.

A full adder is capable of adding three binary digits: two operands and a carry-in value. Unlike a half adder, which can only add two digits, the full adder generates two outputs: the sum and the carry-out. The ripple carry adder, on the other hand, is constructed by chaining multiple full adders, where the carry-out of each stage becomes the carry-in for the next. This sequential process enables multi-bit addition but also introduces propagation delays due to the ripple effect, where carry propagation across stages slows down the operation..

Reversible logic has gained attention in recent years due to its potential to reduce energy dissipation in digital circuits. In reversible logic, the inputs and outputs of each gate must match in number, ensuring a one-to-one correspondence between input and output vectors. This characteristic helps prevent energy loss from irreversible processes and provides a path for low-power circuit design. Reversible gates like the Toffoli gate, Feynman gate, and New gate are key components in designing energy-efficient circuits.

The Toffoli gate, which processes three inputs and produces three outputs, plays a significant role in enhancing the functionality of the ripple carry adder by improving its ability to perform complex logical operations without introducing excessive power dissipation. By utilizing this gate, the circuit becomes

more efficient, reducing energy consumption while maintaining the required computational capability. The Feynman gate, with its simpler design of two inputs and two outputs, is included due to its low quantum cost, making it an ideal choice for minimizing energy usage in simpler operations while still offering reliable results. The New gate, a more sophisticated 3-input, 3-output reversible gate, is incorporated to further optimize the overall power efficiency of the design. By using reversible logic gates, the system avoids the traditional irreversible energy losses associated with standard gates. These gates enable the design to reduce garbage outputs, which are typically unnecessary data bits produced during computation, thus lowering overall energy consumption.

III. PROPOSED METHOD:

In this proposed methodology, the goal is to optimize the full adder design by leveraging reversible logic gates to achieve a balance between performance, power efficiency, and area. The approach utilizes Feynman, Toffoli, and New gates, each with improvements in delay, power consumption, and gate area. The design focuses on minimizing garbage outputs, reducing quantum cost, and ensuring low power dissipation. This is essential for low-power applications in modern computing systems like image processing, cryptography, and signal processing.

By reducing the number of gates required and minimizing the use of Look-Up Tables (LUTs), the design achieves improved area efficiency. Furthermore, the optimization of delay and power consumption ensures that the full adder can meet the demands of high-performance, low-power applications. This approach also makes the design more suitable for implementation in quantum computing, where minimizing energy loss and maintaining system stability are critical. Overall, this method offers a promising solution for energy-efficient, high-speed arithmetic operations in modern computational systems.

Proposed Full Adder Design using Reversible Logic Gates

This proposed methodology focuses on improving the performance and power efficiency of full adder circuits by integrating reversible logic gates such as Feynman, Toffoli, and New gates. The primary objective is to reduce delay, minimize power consumption, and optimize gate area, thereby ensuring better overall efficiency.

1. Feynman Gate Optimization:

The proposed Feynman gate shows minimal delay increase (0.757 ns to 0.761 ns) and maintains the same power consumption (0.082 watts) with minimal LUT usage (1), optimizing efficiency for low-power designs.

2. Toffoli Gate Enhancement:

The Toffoli gate reduces delay from 0.889 ns to 0.761 ns, improving speed without increasing power consumption (0.082 watts) or LUT usage (1), thus enhancing overall performance..

3. New Gate Efficiency:

The New gate reduces delay from 0.893 ns to 0.761 ns, keeps power consumption at 0.082 watts, and optimizes LUT usage (from 2 to 1), improving both speed and energy efficiency.

4. Full Adder Circuit Integration:

Integrating the optimized Feynman, Toffoli, and New gates reduces garbage outputs, quantum cost, and power dissipation, enhancing the full adder's performance for efficient low-power applications.

Performance Evaluation and Optimization :

The proposed full adder design achieves reduced delay, low power consumption, and minimized area through LUT optimization, improving performance for applications in quantum computing and embedded systems.

IV. ADVANTAGES:

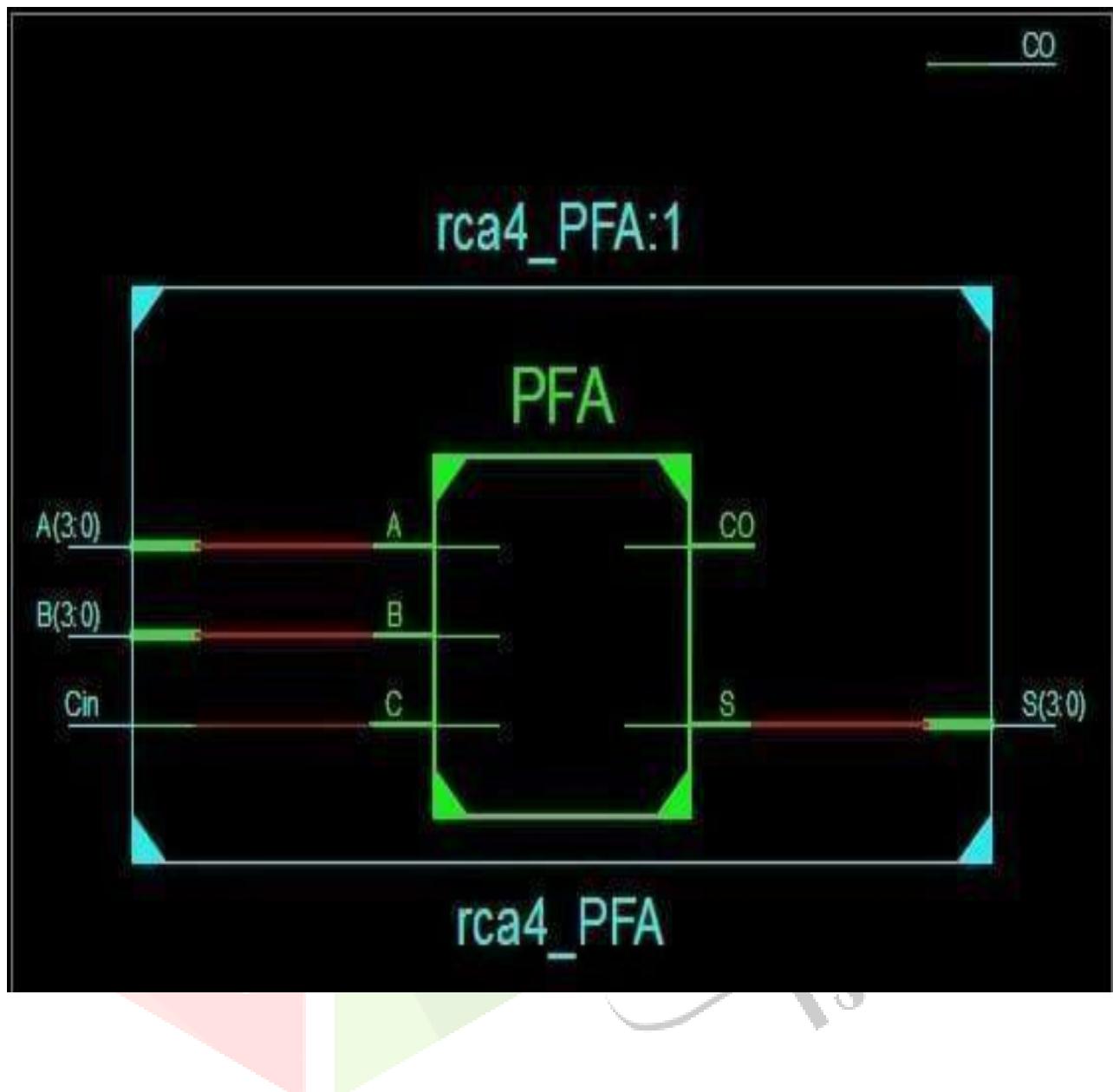
- ⊕ Reduced Energy Consumption: Significantly lowers energy loss, improving the overall energy efficiency of the design.
- ⊕ Enhanced Reliability: Optimized power and thermal performance ensure longer device lifespan and reliable operation.
- ⊕ Low Power Dissipation: Efficient logic gates reduce power consumption, making the design suitable for low-power digital applications and systems.
- ⊕ Cost-Effective: By reducing power consumption and minimizing cooling requirements, the design lowers overall system costs, making it more affordable for widespread use in various applications.
- ⊕ Improved Performance: Optimized delay and low power consumption enhance computational speed and system performance in digital operations.
- ⊕ Compact Design: Fewer gates and LUTs create a more compact design, ideal for embedded systems and space-constrained applications.
- ⊕ Scalability: The design can be easily expanded to higher-bit adders or larger systems without compromising performance or efficiency.

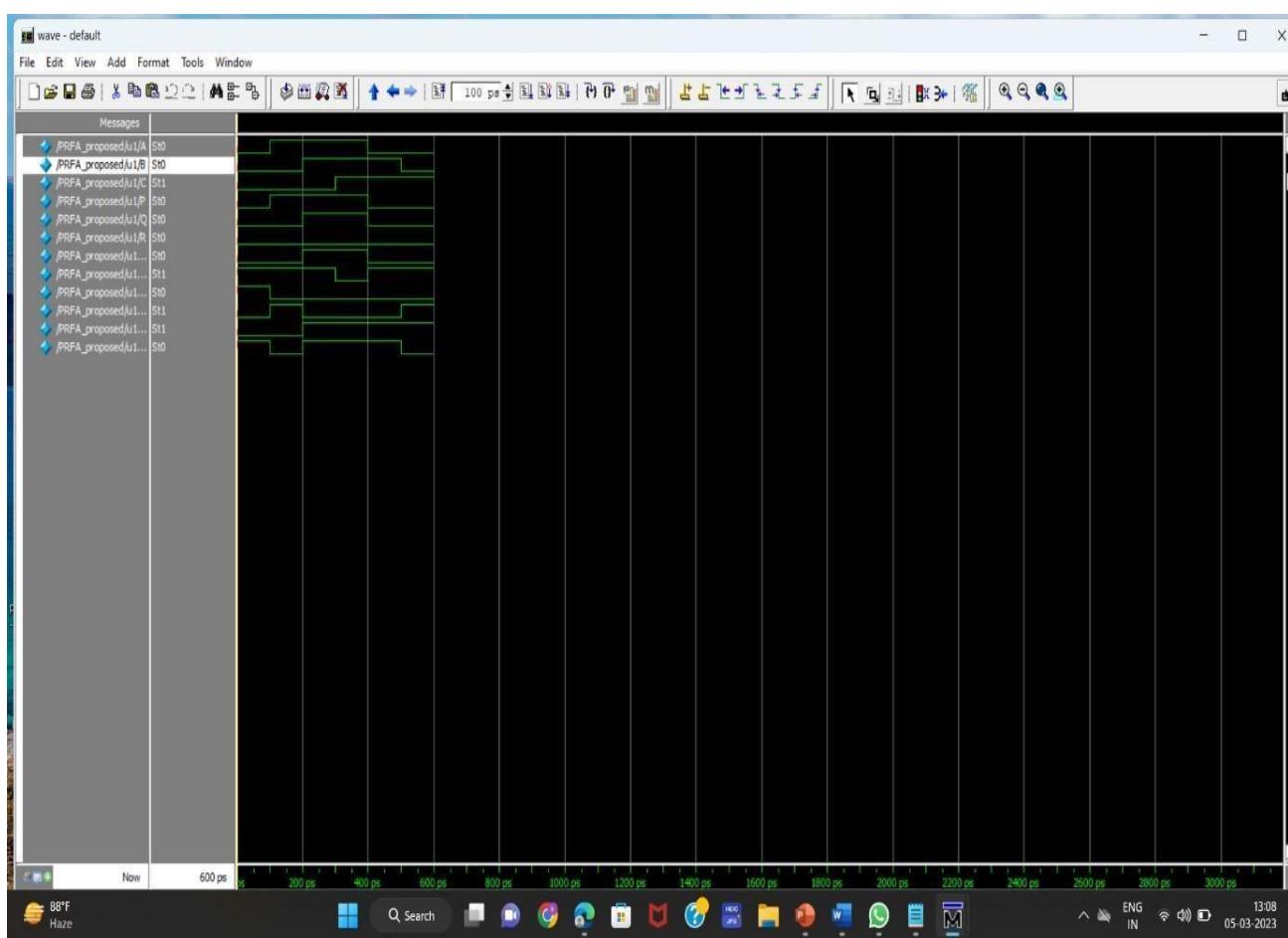
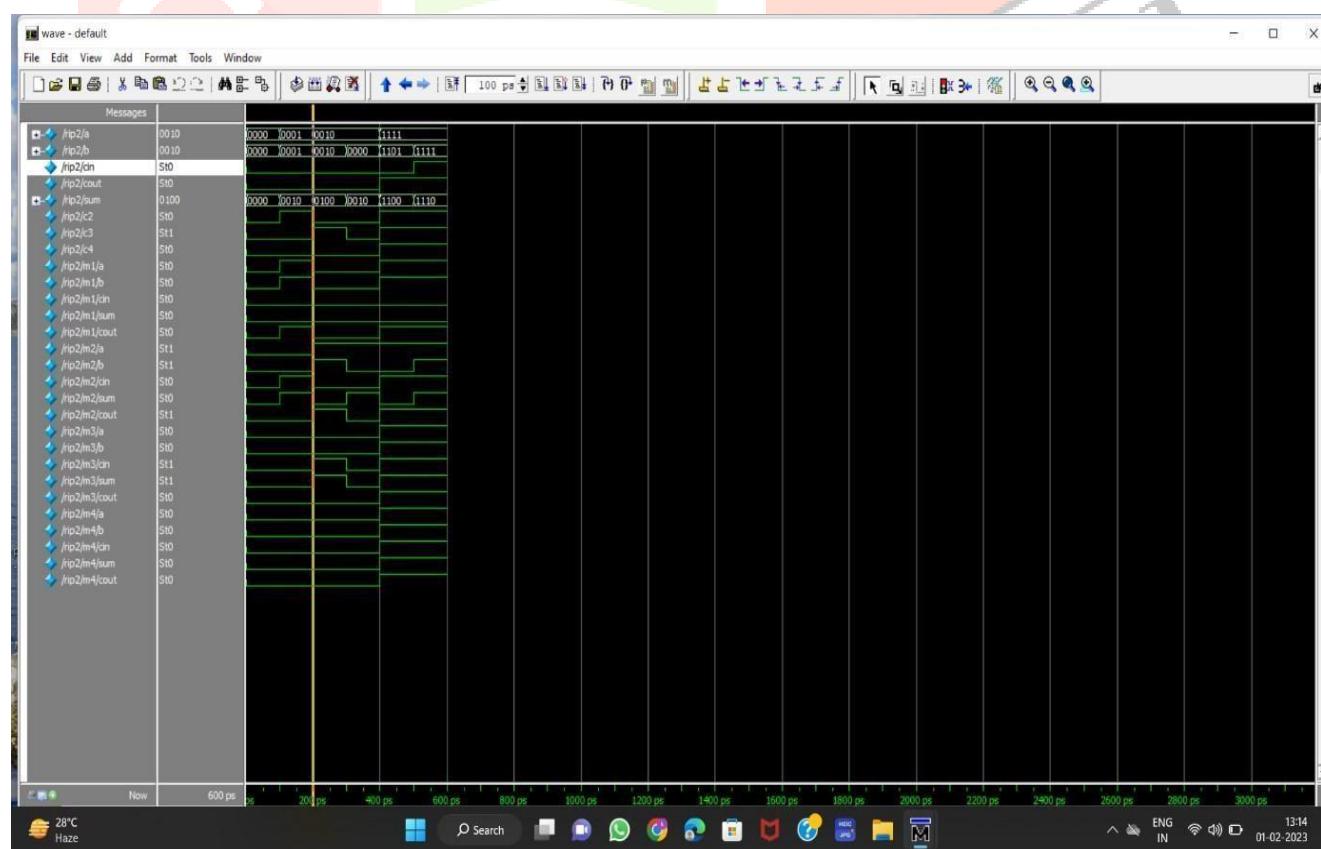
V. APPLICATIONS:

- ⊕ Smart Devices: Optimizes energy efficiency in devices like smartphones and wearables extending battery life and improving performance for everyday use.
- ⊕ IOT Networks: Ideal for energy-efficient IOT applications, reducing power consumption and extending the longevity of connected devices in remote environments.
- ⊕ Embedded Systems: Suitable for use in automotive, healthcare, and industrial applications, offering low-power, high-performance solutions that meet stringent system requirements..
- ⊕ Cloud and Data Centers: Enhances energy usage in server farms and data infrastructure, helping reduce operational costs and promoting sustainable, low-power computing.
- ⊕ High-Performance Computing (HPC): Supports energy-conscious HPC setups, balancing performance and power efficiency for demanding computational tasks.
- ⊕ In-Vehicle Electronics: Powers efficient operation in automotive systems, including infotainment and advanced driver assistance systems (ADAS), ensuring low power consumption.
- ⊕ Portable Electronics: Boosts performance and battery efficiency in portable devices like laptops, tablets, and wearables, enhancing overall runtime through power-saving mechanisms.

VI. RESULTS:

RTL Schematic:



Simulation:**FIG (1): Full Adder Simulation****FIG (2): Ripple Carry Adder Simulation**

Area:**Area Table**

Name	Slice LUTs (134600)	Slice (33650)	LUT as Logic (134600)	Bonded IOB (400)
Reversible ALU	212	72	212	0
Reversible Full Adder	68	22	68	0
Ripple Carry Adder (RC)	144	50	144	0

Delay:**Max Delay Paths**

Slack: inf

Source: x[0] (input port)

Destination: sum[3] (output port)

Path Group: (none)

Path Type: Maximum at Slow Process Corner

Data Path Delay: 19.452ns (41.76%)

Logic Levels: 34

(CARRY4=8, LUT2=6, LUT3=7, LUT4=8),

LUT6=5)

Power:

Parameter	Value
Total On-Chip Power	3.745 W
Design Power Budget	Not Specified
Power Margin	N/A
Junction Temperature	32.7°C
Thermal Margin	47.3°C (Max: 80°C)
Effective SJA	1.85°C/W
Off-Chip Device Power	0 W
Confidence Level	High

Evaluation table for Area, Delay:**Summary Table**

Module	Slice LUTs	Slice Count	Max Delay (ns)	Total Power (W)
Full Adder	68	22	6.283	1.129
Ripple Carry Adder	144	50	13.169	2.616
Reversible ALU (Combinational)	212	72	19.452	3.745

VII. CONCLUSION

The integration of reversible logic gates in Full Adders and Ripple Carry Adders brings notable improvements in both performance and efficiency. By utilizing these gates, the delay associated with computations is significantly reduced, leading to faster operations. Moreover, these gates optimize the area of the circuit, reducing the number of resources required compared to traditional logic gates. The reduction in both delay and area contributes to overall improvements in the adder's functionality and its ability to handle complex computations efficiently. This makes the design of digital systems more compact and high-performing, especially in energy-conscious applications.

Reversible logic, being free from power loss caused by information erasure, plays a crucial role in minimizing energy consumption. This characteristic is particularly beneficial in low-power digital designs where energy efficiency is a critical factor. The ability to conserve power while ensuring reliable functionality makes reversible logic an essential technology for modern computing systems.

Such power-saving properties are especially valuable in advanced fields like quantum computing and nanotechnology, where energy management is key to system performance. Furthermore, in low-power CMOS designs, reversible logic is crucial for reducing the overall power budget while maintaining high computational accuracy.

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